



# Cambridge International AS & A Level

CANDIDATE  
NAME

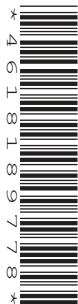
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## FURTHER MATHEMATICS

9231/31

Paper 3 Further Mechanics

October/November 2020

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

## INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity ( $g$ ) is needed, use  $10 \text{ ms}^{-2}$ .

## INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **16** pages. Blank pages are indicated.



















6 Two smooth spheres  $A$  and  $B$  have equal radii and masses  $m$  and  $2m$  respectively. Sphere  $B$  is at rest on a smooth horizontal floor. Sphere  $A$  is moving on the floor with velocity  $u$  and collides directly with  $B$ . The coefficient of restitution between the spheres is  $e$ .

(a) Find, in terms of  $u$  and  $e$ , the velocities of  $A$  and  $B$  after the collision. [3]

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Subsequently,  $B$  collides with a fixed vertical wall which makes an angle  $\theta$  with the direction of motion of  $B$ , where  $\tan \theta = \frac{3}{4}$ .

The coefficient of restitution between  $B$  and the wall is  $\frac{2}{3}$ . Immediately after  $B$  collides with the wall, the kinetic energy of  $A$  is  $\frac{5}{32}$  of the kinetic energy of  $B$ .

(b) Find the possible values of  $e$ . [7]

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